

ECO241 Homework Questions: Chapter 3: Equilibrium Analysis in Economics

1. Find P^* and Q^* for the following model:

$$Q_d = a - bP$$

$$Q_s = -c + dP$$

$$Q_d = Q_s$$

2. Find P^* and Q^* for the following model by (a) elimination of variables and (b) using formulas derived in Question 1.

$$Q_d = 24 - 2P$$

$$Q_s = -5 + 7P$$

$$Q_d = Q_s$$

3. Find the equilibrium P^* and Q^* for the following model:

$$Q_d = 3 - P^2$$

$$Q_s = 6P - 4$$

$$Q_d = Q_s$$

4. Find the equilibrium P^* and Q^* for the following model:

$$Q_d = 8 - P^2$$

$$Q_s = P^2 - 2$$

$$Q_d = Q_s$$

5. The demand and supply functions of a two-commodity market model are as follows:

$$Q_{d1} = 18 - 3P_1 + P_2$$

$$Q_{d2} = 12 + P_1 - 2P_2$$

$$Q_{s1} = -2 + 4P_1$$

$$Q_{s2} = -2 + 3P_2$$

(a) Find P_i^* and Q_i^* ($i = 1, 2$).

(b) Comment on the relationship between Good 1 and Good 2 (Substitute/Complement).

6. The demand and supply functions for a two-commodity market model are as follows:

$$Q_{d1} = 10 - 2P_1 + P_2$$

$$Q_{d2} = 20 + P_1 - P_2$$

$$Q_{s1} = -5 + 6P_1$$

$$Q_{s2} = -2 + 4P_2$$

(a) Find P_i^* and Q_i^* ($i = 1, 2$).

(b) Comment on the relationship between Good 1 and Good 2 (Substitute/Complement).

7. In a two-commodity market equilibrium model, the inverse demand functions are given as

$$P_1 = Q_1^{-\frac{1}{3}} Q_2^{\frac{2}{3}}$$

$$P_2 = Q_1^{\frac{2}{3}} Q_2^{-\frac{1}{3}}$$

(a) Find the demand functions for good 1 and good 2.

(b) Give the supply functions given as follows, find P_i^* and Q_i^* ($i = 1, 2$).

$$Q_1^s = \frac{1}{100} P_1$$

$$Q_2^s = P_2$$

8. Given the following model:

$$Y = C + I_0 + G_0$$

$$C = a + b(Y - T) \quad (a > 0, 0 < b < 1) \text{ [T: taxes]}$$

$$T = d + tY \quad (d > 0, 0 < t < 1) \text{ [t: income tax rate]}$$

(a) How many endogenous variables are there?

(b) Find Y^* , T^* and C^* .

9. Let the national income model be:

$$Y = C + I_0 + G$$

$$C = a + b(Y - T_0) \quad (a > 0, 0 < b < 1)$$

$$G = gY \quad (0 < g < 1)$$

(a) How many endogenous variables are there?

(b) Find Y^* , T^* and C^* .

(c) What restriction on the parameters is needed for a solution to exist?

10. Find Y^* and C^* from the following:

$$Y = C + I_0 + G_0$$

$$C = 30 + 5Y^{1/2}$$

$$I_0 = 20$$

$$G_0 = 15$$