

2

$$\begin{aligned}
 a &= 1 \\
 b &= 1 \\
 c &= -2 \\
 X &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\
 &= \frac{-1 \pm \sqrt{1 - 4(1)(-2)}}{2} = \frac{-1 \pm 3}{2}
 \end{aligned}$$

$$\begin{cases}
 X_1 = -2 \\
 X_2 = 1
 \end{cases}$$

(b) $2X^3 + 11X^2 - 7X - 6 = 0$

Step 1
Rational
Root
Theorem

a_n "a"
 $a \in \{\pm 1, \pm 2, \pm 3, \pm 6\}$
 $b \in \{\pm 1, \pm 2\}$

$\frac{a}{b} \in \{\pm 1, \pm 2, \pm 3, \pm 6, \pm \frac{3}{2}, \pm \frac{1}{2}\}$

Try $X = 1$

$2(1) + 11 - 7 - 6 = 0 \checkmark$

All in the
Candidates!

Step 2. Polynomial Division

$$(2X^3 + 11X^2 - 7X - 6) \div (X - 1) = 2X^2 + 13X + 6$$

$$\begin{array}{r}
 -2X^3 + 2X^2 \\
 \hline
 13X^2 - 7X \\
 13X(X - 1) \\
 \hline
 -13X^2 + 13X \\
 6(X - 1) \\
 \hline
 -6X + 6 \\
 \hline
 0
 \end{array}$$

Step 3. Quadratic Formula

$$\begin{aligned}
 2X^2 + 13X + 6 &= 0 \\
 a &= 2 \\
 b &= 13 \\
 c &= 6 \\
 X &= \frac{-13 \pm \sqrt{(13)^2 - 4(2)(6)}}{4} = \frac{-13 \pm 11}{4} \\
 X_1 &= \frac{-24}{4}, X_2 = \frac{-2}{4} \\
 &= -6 \qquad \qquad = -\frac{1}{2}
 \end{aligned}$$

$$\begin{cases}
 X_0 = 1 \\
 X_1 = -6 \\
 X_2 = -\frac{1}{2}
 \end{cases}$$

Plug in to the original fn: $2(-6)^3 + 11(-6)^2 - 7(-6) - 6 = 0$

$2(-\frac{1}{2})^3 + 11(-\frac{1}{2})^2 - 7(-\frac{1}{2}) - 6 = 0$